



## On Soft bc-Open Sets in Soft Topological Spaces

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### Abstract

In this paper, we offer and study a novel type of generalized soft-open sets in soft topological spaces, named soft bc-open sets. Relationships of this set with other types of generalized soft-open sets are discussed, definitions of soft bc-neighborhood, soft bc-closure and soft bc-interior are introduced, and its properties are investigated. Also, we introduce and explore several characterizations and properties of this type of sets.

**Keywords:** soft b-open set, soft bc-open set, soft bc-nbd, soft bc-interior, soft bc-closure.

### حول المجموعات المفتوحة الناعمة - bc في الفضاءات التوبولوجية الناعمة

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### الخلاصة

في هذا البحث قدمنا ودرشنا نوع جديد من المجموعات المفتوحة الناعمة اسمها (المجموعات المفتوحة الناعمة نوع bc) وقد ناقشنا علاقاتها مع الانواع الاخرى المعروفة من المجموعات المفتوحة الناعمة، كذلك قدمنا تعريفا لكل من الجوارات من النمط bc، انغلاق مجموعة من النمط bc وداخل مجموعة من النمط bc ودرشنا خواصها. كما وجدنا العديد من الخواص والتمييزات للمجموعات الناعمة -bc.

### 1. Introduction and Preliminaries

The concept of soft set theory was instigated and applied by Molodtsov [1,2] as a mathematical device for dealing with uncertainties. In a previous work [3], Shaber and Naz defined soft topological spaces and soft open sets. Soft  $\beta$ -open sets were introduced and studied by several authors, including the soft  $\alpha$ -open [4], soft preopen [5], soft semi open [4], and soft regular open sets [6]. In another study [7], Akdag and Ozkan realized the soft b-open sets and soft continuity. The concept of bc-open sets was introduced by Ibrahim [8].

Let  $(Z, \tau, A)$  be a soft topological space, where  $A$  is any set of parameters. The soft closure (resp. soft interior) [9] of a soft set  $(P, A)$  is denoted by  $(cl(P, A))$  (resp.  $(int(P, A))$ ). A subset  $(P, A)$  is said to be a  $\beta$ -open [4] (resp. soft  $\alpha$ -open [5], soft preopen [4], soft semi-open [6] and soft regular) set, if:  $(P, A) \subset cl(int(cl((P, A))))$  (resp.  $(P, A) \subset int(cl(int((P, A))))$ ),  $(P, A) \subset int(cl((P, A)))$ ,  $(P, A) \subset cl(int((P, A)))$  and  $(P, A) = int(cl((P, A)))$ .

We denote the family of all soft sets over  $X$  by  $SS(Z, A)$ .

**Definition 1.1**[3]. Let  $\tau$  be a collection of soft open sets over  $Z$ , then  $\tau$  is said to be soft topological space if (1)  $\emptyset$  and  $\tilde{X}$  belong to  $\tau$ , (2) The union of any subcollection

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of soft sets of  $\tau$  belongs to  $\tau$ , and (3) the intersection of any two soft sets in  $\tau$  belongs to  $\tau$ . We named the triple  $(Z, \tau, A)$  by **STS**.

**Definition 1.2** [9]. The soft set  $(P, A) \in SS(Z, A)$  is called a *soft point* in  $Z$ , denoted by  $e_L$ , if for the element  $e \in A$ ,  $F(e) \neq \emptyset$  and  $F(e') = \emptyset$  for all  $e' \in A \setminus \{e\}$ . The set of all soft points of  $Z$  is denoted by  $SP(Z)$ .

**Definition 1.3** [7]. If  $(P, A) \in SS(Z, A)$  then it is called

(1) Soft **b** – open set (briefly *sb – open set*), iff  $(P, A) \subset \text{int}(\text{cl}((P, A))) \cup \text{cl}(\text{int}((P, A)))$ .

(2) Soft **b** – closed (briefly *sb – closed*) set, iff  $(P, A) \supset \text{int}(\text{cl}((P, A))) \cap \text{cl}(\text{int}((P, A)))$ .

**Definition 1.4** [6,7]. Let  $(P, A)$  be a soft set of a **STS**  $(Z, \tau, A)$ , then

(1) Soft *semi – interior* of a soft set  $(P, A)$  in  $Z$  is denoted by

$$sSint((P, A)) = \cup \{(W, A) : (W, A) \text{ is a soft semi-open set and } (W, A) \subset (P, A)\}.$$

(2) Soft *semi – closure* of a soft set  $(P, A)$  in  $Z$  is denoted by

$$sScl((P, A)) = \cap \{(L, A) : (L, A) \text{ is a soft semi-closed set and } (P, A) \subset (L, A)\}.$$

(3) Soft **b** – interior of a soft set  $(P, A)$  in  $Z$  is denoted by

$$sbint((P, A)) = \cup \{(W, A) : (W, A) \text{ is a soft b-open set and } (W, A) \subset (P, A)\}.$$

(4) Soft **b** – closure of a soft set  $(P, A)$  in  $Z$  is denoted by

$$sbcl((P, A)) = \cap \{(L, A) : (L, A) \text{ is a soft b-closed set and } (P, A) \subset (L, A)\}.$$

Clearly,  $sbcl(P, A)$  (resp.  $sScl(P, A)$ ) is the smallest soft **b**-closed (resp. soft semi-closed) set over  $Z$  which contains  $(P, A)$ , and  $sbint((P, A))$  (resp.  $sSint((P, A))$ ) is the largest soft **b**-open (resp. semi-open) set over  $Z$  which is contained in  $(P, A)$ .

We will denote the family of all soft **b**-open (resp., soft semi-open) sets and soft **b**-closed ((resp., soft semi-closed) sets of a soft topological space by  $bO(Z)$  (resp.,  $SSO(Z)$ )  $SbC(Z)$  (resp.,  $SSC(Z)$ ).

**Definition 1.5** [10]. Let  $(Z, \tau, A)$  be a **STS**. and  $x, y \in Z$ , such that  $x \neq y$ . If there exist soft open sets  $(P, A)$  and  $(S, A)$ , such that  $x \in (P, A), y \notin (S, A), y \in (S, A)$ , and  $x \notin (P, A)$ , then  $(Z, \tau, A)$  is called a soft  $T_1$ -space.

**Theorem 1.6** [10]. Let  $(Z, \tau, E)$  be **STS**. Then each soft point is a soft closed if and only if  $(Z, \tau, A)$  is a soft  $T_1$ -space.

**Definition 1.7** [11]. An **STS**  $(Z, \tau, A)$  is called a *soft locally indiscrete*, if every soft open set over  $Z$  is a soft closed set over  $Z$ .

## 2. Soft **bc** – open sets

Now, we give a new family of *soft b – open* sets named *soft bc – open* sets in an **STS** and study some of its basic properties.

**Definition 2.1** A subset  $(P, A)$  of **STS**  $(Z, \tau, E)$  is named *soft bc – open* (*sbc – open*) if, for any  $x \in (P, A) \in SbO(Z)$ , there is a soft closed set  $(S, A)$ , such that  $x \in (S, A) \subset (P, A)$ . The complement of  $(P, A)$  is named *soft bc – closed* (*sbc – closed*).

The collection of all soft *bc – open* sets in  $Z$  is denoted by  $SbcO(Z)$  and the collection of all soft *bc – closed* sets in  $Z$  is named  $SbcC(Z)$ .

**Theorem 2.2** A soft subset  $(P, A)$  of **STS**  $(Z, \tau, A)$  is soft *bc – open* iff  $(P, A)$  is *sb – open* and it is a union of soft closed sets.

**Proof.** ( $\Rightarrow$ ) Let  $(P, A)$  be a soft *bc – open* set. Then  $(P, A)$  is *sb – open* set and for each  $x \in (P, A)$  there is a soft closed set  $(L, A)$ , such that  $x \in (L, A) \subseteq (P, A)$ . Then we get  $\cup\{x\}_{x \in (P, A)} = (P, A) \subseteq (L, A) \subseteq (P, A)$ . Thus,  $(P, A) = \cup(L, A)$ , where  $(L, A)$  is a soft closed set for each  $x \in (P, A)$ .

( $\Leftarrow$ ) Direct form the definition of soft *bc – open*.

**Corollary 2.3** For a **STS**  $(Z, \tau, A)$ , if  $(L, A)$  is *sb – open* set over  $X$ , then  $(L, A)$  is an *sbc – open* if  $(L, A)$  is a soft closed set.

**Proposition 2.4** A soft subset  $(H, A)$  of an **STS**  $(Z, \tau, A)$  is *sbc – closed* if and only if  $(H, A)$  is a soft *b – closed* set and it is an intersection of soft open sets.

**Proof.** It is obvious.

**Remark 2.5** Every *sbc – open* set of a space  $Z$  is soft *b – open*, but the converse is not true in general, as shown by the following example.

**Example 2.6** Let  $Z = \{v_1, v_2, v_3\}, A = \{e_1, e_2, e_3\}$  and

$$\tau = \{\emptyset, \overline{Z}, (P_1, A), (P_2, A), (P_3, A), (P_4, A)\}$$

where  $(P_1, A), (P_2, A), (P_3, A), (P_4, A)$  are soft sets over  $Z$ , defined as follows:

$$(P_1, A) = \{(e_1, \widetilde{Z}), (e_2, \{v_2, v_3\}), (e_3, \{v_1, v_2\})\},$$

$$(P_2, A) = \{(e_1, \widetilde{\emptyset}), (e_2, \{v_1\}), (e_3, \{v_3\})\},$$

$$(P_3, A) = \{(e_1, \{v_2\}), (e_2, \{v_1, v_3\}), (e_3, \{v_3\})\},$$

$$(P_4, A) = \{(e_1, \{v_2\}), (e_2, \{v_3\}), (e_3, \widetilde{\emptyset})\}.$$

Then,  $\tau$  defines a soft topology on  $Z$ .

The soft closed sets are  $\widetilde{Z}, \widetilde{\emptyset}, (P_1, A)^c, (P_2, A)^c, (P_3, A)^c, (P_4, A)^c$ ,

where  $(P_1, A)^c = \{(e_1, \widetilde{\emptyset}), (e_2, \{v_1\}), (e_3, \{v_3\})\} = (P_2, A)$

$(P_2, A)^c = \{(e_1, \widetilde{Z}), (e_2, \{v_2, v_3\}), (e_3, \{v_1, v_2\})\} = (P_1, A)$

$(P_3, A)^c = \{(e_1, \{v_1, v_3\}), (e_2, \{v_2\}), (e_3, \{v_1, v_2\})\},$

$(P_4, A)^c = \{(e_1, \{v_1, v_3\}), (e_2, \{v_2, v_3\}), (e_3, \widetilde{Z})\}.$

The family of  $SbOS(Z) = \{(P_1, A), (P_2, A), (P_3, A), (P_4, A)\}.$

The family of  $SbcOS(Z) = \{(P_1, A), (P_2, A), (P_3, A)\}.$

Then  $(P_4, A) \in SbOS(Z)$ , but  $(P_4, A) \notin SbcOS(Z)$ .

By Remark (2) [8] and the above Remark (2.5), we have the following implications:

Soft regular set  $\Rightarrow$  Soft -open set  $\Rightarrow$  Soft  $\alpha$  -open set  $\Rightarrow$  Soft *semi* -open set

$\Downarrow$

Soft *pre* -open set  $\Rightarrow$  Soft  $\check{b}$  -open set  $\Rightarrow$  Soft  $\beta$  -open set

$\Uparrow$

Soft  $\check{bc}$  -open set

**Proposition 2.7** An arbitrary union of *sbc* - open sets is *sbc* - open set.

**Proof.** Suppose that  $\{(P, A)_\lambda : \lambda \in \Delta\}$  is a family of soft *bc* - open sets in  $(Z, \tau, A)$ . Then  $(P, A)_\lambda$  is soft *b* - open set for each  $\lambda \in \Delta$ . So,  $\cup(P, A)_\lambda$  is soft *b* - open. Let  $x \in \cup\{(P, A)_\lambda : \lambda \in \Delta\}$ , so  $x \in (L, A)_\lambda$  for some  $\lambda \in \Delta$ . Since  $(P, A)_\lambda$  is soft *b* - open for each  $\lambda$ , then there is a soft closed set  $(L, A)$  such that

$x \in (L, A) \subset (P, A)_\lambda \subset \cup\{(P, A)_\lambda : \lambda \in \Delta\}$ , so  $x \in (L, A) \subset \cup\{(P, A)_\lambda : \lambda \in \Delta\}$ . Therefore,  $\cup\{(P, A)_\lambda : \lambda \in \Delta\}$  is soft *bc* - open set.

Now we show that the intersection of two *sbc*- open sets is not necessarily *sbc*- open.

**Example 2.8.** Let the *STS*  $(Z, \tau, A)$  as in Example 2.6, then  $(P_1, A) \in SbcO(Z)$  and  $(P_3, A) \in SbcO(Z)$ , but  $(P_1, A) \cap (P_3, A) = (P_4, A) \notin SbcO(Z)$ .

**Remark 2.9.** From the above example we notice that the family of all *sbc* - open subset of a space  $Z$  is a supra topology and thus it is not a topology in general.

The following result gives a condition under which the family of all *sbc* - open sets became a topology on  $Z$ .

**Proposition 2.10.** If the collection  $SbO(Z)$  is a topology on  $Z$ , then  $SbcO(Z)$  is also a topology on  $Z$ .

**Proof.** It is clear that  $\widetilde{\emptyset}, \widetilde{Z} \in SbcO(Z)$  and, by Proposition 2.7, the union of any subset of  $SbcO(Z)$  is *sbc* - open. Now, let  $(P, A)$  and  $(S, A)$  be two *sbc* - open sets, then  $(P, A)$  and  $(S, A)$  are soft *b* - open sets. Since  $SbO(Z)$  is a topology on  $Z$ , so  $(P, A) \cap (S, A)$  is soft *b* - open. If  $x \in (S, A) \cap (P, A)$ , then  $x \in (P, A)$  and  $x \in (S, A)$ . So there exist two soft closed sets  $(L, A)$  and  $(K, A)$ , such that  $x \in (L, A) \subset (S, A)$  and  $x \in (K, A) \subset (P, A)$ . This implies that  $x \in (L, A) \cap (K, A) \subset (S, A) \cap (P, A)$ . Since any intersection of soft closed sets is soft closed, then  $(L, A) \cap (K, A)$  is a closed set. Thus,  $(P, A) \cap (S, A)$  is *sbc* - open set.

**Theorem 2.11** A soft set  $(P, A)$  of a *STS*  $(Z, \tau, A)$  is a soft *bc* - open set iff, for each  $x \in (P, A)$ , there is a soft *sbc* - open set  $(S, A)$  such that  $x \in (S, A) \subseteq (P, A)$ .

**Proof.** Suppose that  $(P, A)$  is soft *bc* - open in the space  $Z$ , then for each  $x \in (P, A)$ , put  $(P, A) = (S, A)$  is *sbc* - open set containing  $x$  such that  $x \in (P, A) \subseteq (S, A)$ .

Conversely, assume that for any  $x \in (P, A)$ , there is a *sbc* - open set  $(S, A)$  such that  $x \in (S, A) \subseteq (P, A)$ . Thus,  $(P, A) = \cup(S, A)_x$  where  $(S, A)_x \in SbcO(Z)$  for each  $x$ . Hence,  $(P, A)$  is *sbc* - open set.

**Theorem 2.12** Let  $(Z, \tau, A)$  be soft  $T_1$  – space, then  $(P, A)$  is  $sb$  – open set iff  $(P, A)$  is a soft  $bc$  – open.

**Proof** Suppose that  $(Z, \tau, A)$  is soft  $T_1$  – space and  $(P, A)$  is  $sb$  – open set. If  $(P, A) = \tilde{\emptyset}$ , then  $(P, A) \in sbc(Z)$ . If  $(P, A) \neq \tilde{\emptyset}$ , let  $x \in (P, A)$ . Since  $(Z, \tau, A)$  is soft  $T_1$  – space, then by Theorem 1.6, each soft point is a closed set and, hence,  $x \in \{x\} \subset (P, A)$ . Therefore,  $(P, A)$  is an  $sbc$  – open, thus  $SbO(Z) \subset SbcO(Z)$ . But  $SbcO(Z) \subset SbO(Z)$ . Hence,  $SbO(Z) = SbcO(Z)$ .

**Proposition 2.13** If  $(Z, \tau, A)$  is soft locally indiscrete, then  $SSO(Z) \subset SbcO(Z)$ .

**Proof.** Let  $(P, A)$  be any soft subset of  $STS(Z, \tau, A)$  and  $(P, A) \in SSO(Z)$ , if  $(P, A) = \tilde{\emptyset}$ , then  $(P, A) \in SbcO(Z)$ . If  $(P, A) \neq \tilde{\emptyset}$ , then  $(P, A) \subset cl(int((P, A)))$ . Since  $(Z, \tau, A)$  is soft locally indiscrete, then  $int(P, A)$  is soft closed, so  $int(P, A) \subset (P, A)$ . This implies that for each  $x \in (P, A)$ ,  $x \in (int(P, A)) \subset (P, A)$ . Therefore,  $(P, A)$  is  $sbc$  – open set. Hence  $SSO(Z) \subset SbcO(Z)$ .

**Theorem 2.14** Let  $\{(P, A)_\alpha : \alpha \in \Delta\}$  be a collection of  $sbc$  – closed sets in a soft topological space  $(Z, \tau, A)$ . Then  $\bigcap \{(P, A)_\alpha : \alpha \in \Delta\}$  is soft  $bc$  – closed.

**Proof.** The proof follows from Proposition 2.7.

### 3. Some Properties of Soft $bc$ – Open Sets

In this section, we provide some soft topological operations on soft sets and discuss its properties.

**Definition 3.1** Let  $(Z, \tau, A)$  be an  $STS$  and  $x \in \tilde{Z}$ . Then, a soft set  $(P, A)$  is said to be soft  $bc$  – neighborhood (briefly, soft  $bc$  –  $nbh$ ) of  $x$ , if there exists a soft  $bc$  – open set  $(K, A)$  over  $Z$  such that  $x \in (K, A) \subset (P, A)$ .

**Proposition 3.2** For an  $STS (Z, \tau, A)$ , a soft set  $(P, A)$  is  $sbc$  – open iff it is a soft  $bc$  – neighborhood of each of its points.

**Proof.** Let  $(P, A) \in \tilde{Z}$  be a soft  $sbc$  – open set, since for every  $x \in (P, A)$ ,  $x \in (P, A) \subset (P, A)$  and  $(P, A)$  is  $sbc$  – open, this shows that  $(P, A)$  is a soft  $bc$  – neighborhood of each of its points.

Conversely, suppose that  $(P, A)$  is a soft  $bc$  – neighborhood of each of its points. Then for each  $x \in (P, A)$ , there exists  $(S, A)_x \in SbcO(Z)$  such that  $(S, A)_x \subset (P, A)$ . Then  $(P, A) = \bigcup \{(S, A)_x : x \in (P, A)\}$ . Since each  $(S, A)_x$  is  $sbc$  – open. It follows that  $(P, A)$  is  $sbc$  – open.

**Proposition 3.3** Every soft  $bc$  – neighborhood of a point is soft  $b$  – neighborhood.

**Proof.** It is obvious from the fact that every  $sbc$  – open set is  $sb$  – open.

**Definition 3.4** Let  $(P, A)$  be soft set of a  $STS (Z, \tau, A)$ , then a point  $x \in Z$  is called soft  $bc$  – interior point of  $(P, A)$ , if there exists an  $sbc$  – open set  $(U, A)$  such that  $x \in (U, A) \subset (P, A)$ . The set of all  $sbc$  – interior points of  $(P, A)$  is denoted by  $sbcInt(P, A)$ .

**Proposition 3.5** Let  $(P, A)$  be a soft set of  $Z$ , then  $sbcInt(P, A) \subset sbInt(P, A)$ .

**Proof.** Since  $sbc$  – open set is  $sb$  – open, so the proof holds.

**Definition 3.6** Let  $(P, A)$  be a soft set of a  $STS(Z, \tau, A)$ , then the soft  $bc$  – closure of  $(P, A)$ , denoted by  $sbcCl(P, A)$ , is the intersection of all  $sbc$  – closed sets containing  $(P, A)$ .

In the following theorem we provide some properties of  $sbc$  – interior of a soft set.

**Theorem 3.7** Let  $(Z, \tau, A)$  be  $STS$  and let  $(P, A)$  and  $(M, A)$  be soft sets over  $Z$ . Then

- 1)  $sbcInt(P, A)$  is the union of all  $sbc$  – open sets which are contained in  $(P, A)$ .
- 2)  $sbcInt(P, A)$  is  $sbc$  – open set in  $Z$ .
- 3)  $(P, A)$  is  $sbc$  – open iff  $(P, A) = sbcInt(P, A)$ .
- 4)  $sbcInt(sbcInt(P, A)) = sbcInt(P, A)$ .
- 5)  $sbcInt(\tilde{\emptyset}) = \tilde{\emptyset}$  and  $sbcInt(\tilde{Z}) = \tilde{Z}$ .
- 6)  $sbcInt(P, A) \subset (P, A)$ .
- 7) If  $(P, A) \subset (M, A)$ , then  $sbcInt(P, A) \subset sbcInt(M, A)$ .
- 8) If  $(P, A) \cap (M, A) = \tilde{\emptyset}$ , then  $sbcInt(P, A) \subset sbcInt(M, A)$ .
- 9)  $sbcInt(P, A) \cup sbcInt(M, A) \subset sbcInt((P, A) \cup (M, A))$ .
- 10)  $sbcInt((P, A) \cap (M, A)) \subset sbcInt(P, A) \cap sbcInt(M, A)$ .

**Proof.** The proofs of these facts are easy, so we will only prove the point number 7:

Suppose that  $x \in Z$ ,  $x \in sbcInt(P, A)$ , then by Definition 3.4, there is a set  $(U, A)$  such that  $x \in (U, A) \subset (P, A) \subset (M, A)$ , thus  $x \in sbcInt(M, A)$ .

**Theorem 3.8** Let  $(P, A)$  be any soft set in a **STS**  $(Z, \tau, A)$ , then  $x \in sbcCl(Z)$  if and only if  $(P, A) \cap (U, A) = \emptyset$  for any *sbc* – open set  $(U, A)$  containing  $x$ .

**Proof.**( $\Rightarrow$ ) let  $x \in sbcCl(P, A)$ . Suppose that  $(P, A) \cap (U, A)_x = \emptyset$ , where  $(U, A)_x \in sbcO(Z)$  containing  $x$ . Hence,  $(P, A) \subset (U, A)_x^c$ , where  $(U, A)_x^c \in sbcC(P, A)$ . Hence,  $x \notin sbcCl(P, A)$ , which is a contradiction.

( $\Leftarrow$ ) Let  $x \notin sbcCl(P, A)$ , then  $x \notin \cap(L, A)$ , where  $(L, A) \in sbcC(Z)$  and  $(P, A) \subset (L, A)$  for each  $(L, A)$ . Hence,  $x \in (\cap(L, A))^c$ , where  $(\cap(L, A))^c \in sbcO(Z)$  containing  $x$ . Now, we have  $(P, A) \cap (\cap(L, A))^c \subset (\cap(L, A)) \cap (\cap(L, A))^c = \emptyset$ .

**Theorem 3.9** Let  $(P, A)$  be any soft subset of an **STS**  $(Z, \tau, A)$  if  $(P, A) \cap (L, A) \neq \emptyset$  for any soft closed set  $(L, A)$  containing  $x$ , then  $x \in sbcCl(P, A)$ .

**Proof.** Suppose that  $(U, A)_x \in sbcO(Z)$  containing  $x$ , then by definition (2.1), there is  $(L, A)$  soft closed set such that  $x \in (L, A) \subset (U, A)$ . So, by the hypothesis,  $(P, A) \cap (L, A) \neq \emptyset$ . Hence,  $(P, A) \cap (U, A) \neq \emptyset$  for any *sbc* – open set  $(U, A)_x$ . Therefore,  $x \in sbcCl(P, A)$ .

**Theorem 3.10.** Let  $(Z, \tau, A)$  be an **STS** and let  $(P, A)$  and  $(M, A)$  be soft sets over  $Z$ . Then

- 1)  $sbcCl(P, A)$  is the intersection of all *sbc* – closed sets which are containing  $(P, A)$ .
- 2)  $(P, A) \subset sbcCl(P, A)$ .
- 3)  $sbcCl(P, A)$  is *sbc* – closed set in  $Z$ .
- 4)  $(P, A)$  is *sbc* – closed iff  $(P, A) = sbcCl(P, A)$ .
- 5)  $sbcCl(sbcCl(P, A)) = sbcCl(P, A)$ .
- 6)  $sbcCl(\tilde{\emptyset}) = \tilde{\emptyset}$  and  $sbcCl(\tilde{Z}) = \tilde{Z}$ .
- 7) If  $(P, A) \subset (M, A)$ , then  $sbcCl(P, A) \subset sbcCl(M, A)$ .
- 8) If  $sbcCl(P, A) \cap sbcCl(M, A) = \tilde{\emptyset}$ , then  $(P, A) \cap (M, A) = \tilde{\emptyset}$ .
- 9)  $sbcCl(P, A) \cup sbcCl(M, A) \subset sbcCl((P, A) \cup (M, A))$ .
- 10)  $sbcCl((P, A) \cap (M, A)) \subset sbcCl(P, A) \cap sbcCl(M, A)$ .

**Proof.** It is obvious.

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#### References

1. Molodtsov, D. **1999**. "Soft set theory-first results," *Computers and Mathematics with Applications*, **37**(4-5): 19-31.
2. Molodtsov, D., Leonov, V.Y. and Kovkov, D.V. **2006**. "Soft sets technique and its application", *Nechetkie Sistemyi Myagkie Vychisleniya*, **1**(1): 8-39.
3. Shabir, M. and Naz, M. **2011**. "On soft topological spaces". *Computers and Mathematics with Applications*, **61**(7): 1786-1799.
4. Arockiarani and Arokialancy, A. **2013**. "Generalized soft  $g\beta$ -closed sets and soft  $gs\beta$ -closed sets in soft topological space", *International Journal of Mathematical Archive*, **4**(2): 1-7.
5. Akdag, M. and Ozkan, A. **2014**. "Soft  $\alpha$ -Open Sets and Soft  $\alpha$ -Continuous Functions". *Abstr. Appl. Anal.* 2014, Article ID 891341, 7 pages. doi:10.1155/2014/891341. <https://projecteuclid.org/euclid.aaa/1412273201>.
6. Chen, B. **2013**. "Soft Semi-open sets and related properties in soft topological spaces," *Applied Mathematics and Information Sciences*, **7**(1): 287-294.
7. Akdag, M. and Ozkan, A. **2014**. "Soft b-open sets and soft b-continuous functions". *Math Sci*, **8**: 124, doi: 10.1007/s40096-014-0124-7.
8. Ibrahim, H. **2013**. "Bc-Open Sets in Topological Spaces", *Advances in Pure Mathematics*, **3**(1): 34-40. doi: [10.4236/apm.2013.31007](https://doi.org/10.4236/apm.2013.31007).
9. Zorlutuna, M., Akdag, W. K. and Atmaca, S. **2012**. "Remarks on soft topological spaces," *Annals of Fuzzy Mathematics and Informatics*, **3**(2): 171-185.
10. Hussain, S. and Ahmad, B. **2015**. "Soft separation axioms in soft topological spaces", *Hacettepe Journal of Mathematics and Statistics*, **44**(3): 559 – 568.
11. Selvi, A. and Arockiarani, I. **2015**. "On Soft slightly  $\pi g$ -continuous functions", *Journal of Progressive Research in Mathematics*, **3**(2): 168-174.