



ISSN: 0067-2904

Studying the Atomic and Molecular Hydrogen Mass (M_{HI} , M_{H_2}) Properties of the Extragalactic Spectra

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Received: 5/8/ 2019

Accepted: 30/9/2020

Abstract

The purpose of this study is to deal with dust and interstellar molecular and atomic gas owing to obtaining a proportion of cold gas to dust and to understand the characteristics of the molecular gas in extragalactic data selected from the Herschel SPIRE/ FTS archive. The physical properties of a sample of 65 extragalactic spectra characterized by the activity of star formation were discussed in this work. Statistical analyses, using STATISTICA program, were made for the content of cold gas (M_{HI} , M_{H_2}), dust mass (M_{dust}), cold temperature of dust (T_d) and luminosities in Far-infrared to CO line radiations, while coefficients of partial correlation within those characteristics were established. The results showed that the molecular hydrogen mass (M_{H_2}) is strongly correlated with the HI or the total gas mass corresponding to the Far-infrared emission (L_{FIR}) resulting from dust in the galaxies molecular clouds. The results also indicated that these kinds of galaxies have large molecular mass as well as high star formation efficiency per unit mass.

Keywords: Galaxies; Interstellar gas; Molecular clouds; Far-Infrared and CO line radiations.

دراسة خصائص كتلة الهيدروجين الذري والجزيئي (M_{H_2} , M_{HI}) لأطياف المجرات الخارجية

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الخلاصة

ان الغرض من هذه الدراسة هو التعامل مع الغبار والغازات الجزيئية والذرية ما بين النجوم وذلك للحصول على نسبة الغاز البارد إلى الغبار وفهم خصائص الغاز الجزيئي من بيانات المجرات الخارجية المختارة من أرشيف Herschel SPIRE / FTS. في هذا العمل تمت مناقشة الخواص الفيزيائية لعينة 65 من أطياف المجرات الخارجية والتي تتميز بفعالية النشوء النجمي. تم إجراء التحليلات لإحصائية لمحتوى الغاز البارد (M_{HI}, M_{H_2})، وكتلة الغبار (M_{dust}) ودرجة الحرارة الباردة للغبار (T_d) وضياءات الأشعة تحت الحمراء البعيدة إلى إشعاعات خط أول اوكسيد الكربون CO، وتم تحديد معاملات الارتباط الجزيئي ضمن تلك الخصائص. التحليلات الإحصائية حصلت عليها باستخدام برنامج STATISTICA. اظهرت النتائج أن كتلة الهيدروجين الجزيئي (M_{H_2}) ترتبط ارتباطاً قوياً مع كتلة الهيدروجين الذري HI أو كتلة الغاز الكلية المقابلة لانبعث الأشعة تحت الحمراء البعيدة (L_{FIR}) الناتج من الغبار الموجود في السحب الجزيئية للمجرات. اشارت النتائج أيضاً إلى أن هذه الأنواع من المجرات تمتلك كتلة جزيئية كبيرة اضافة الى كفاءة نشوء نجمي عالية لكل وحدة كتلة.

Introduction

Galaxies throughout all environments can possess a cold gas component suitable for powering star formation or an active galactic nucleus (AGNs). Studies of local universe galaxies demonstrated that many of them contain important nuclear and molecular cold gas reservoirs [1]. The molecular gas within the multi-phase interstellar medium (ISM) was the most closely tied to star formation rate (SFR), and thus dramatic effects on galaxies evolution are associated with the stellar lifecycle. Even if the dominant component of such gas is molecular hydrogen (H_2), it is difficult to detect pure H_2 rotational lines without being especially sensitive to the cold temperatures of most molecular clouds [2]. The star formation efficiency (SFE) is a crucial component in understanding the history of star formation of galaxies at all redshifts as well as the universe's global evolution [3].

The poor understanding of the physical principles behind the star formation process still restricts our knowledge of galaxies evolution, in other words, the condensation of the primitive gaseous material of HI into H_2 and thus its collapse into stars. The feedback mechanisms caused by the recently born stars on the ISM are also poorly known. The ultraviolet emission field (UVWF) linked with massive star formation causes the nearby gas to be ionized and leads the hydrogen molecules to be photo-dissociated. Supernova winds, furthermore, inject kinetic energy (and metals) into the ISM, causing unique star formation on the shock wave fronts [4]. Far-infrared radiations in these sources are primarily caused by ultraviolet (UV) emission-warmed dust from young and gigantic stars in the neighbor galaxies [5]. A previous study [6] illustrated that massive envelopes of extragalactic emission's ionized hydrogen (HII) with masses that are significantly surpassing the masses of intergalactic HI disks could exist across galaxies in which the dimensions of HI disks exceed those of stellar disks considerably. These enlarged disks could in considerable time scales "feed" the formation rate of stars in their host galaxies. According to a published article [7], the nuclei of active galaxies that are contiguous to molecular gas tend to have considerably redder infrared colors and they cause a lack in molecules of carbon monoxide (CO) detections, revealing duster environments in the CO luminous nuclei.

Evolution observations in the dust-to-metal ratio enable us to restrict the processes of the prevailing dust processing [8]. The forms of HI H_2 are well linked with previous and present indices of star formation rate, such as the brightness of the surface of the blue F_B , Far-infrared F_{FIR} and radio continuum F_R , but the correlation is stronger for the molecular clouds content of M_{H_2} [9], indicating increased molecular hydrogen gas excitation. Findings related to the dust and the atomic and molecular gas mass of these galaxies enable us to investigate their star formation activity and obtain their interstellar gas properties.

This paper is structured according to the following: We describe the characteristics of our observational data details of the 65 extragalactic samples and procedures to evaluate all parameters in Section 2. The results and discussion of our statistical analysis are presented in Section 3. The conclusions drawn from this study are given in Section 4.

Observations Sample and Description Parameters

Sample Selection

The cold gas (atomic + molecular) kinematics for 65 extragalactic spectra samples from an archive of the Herschel SPIRE Fourier Transform Spectrometer (FTS) were studied by means of the statistical analysis of the $M_{H_2}+HI$ masses properties. In particular, cold gas masses-to-luminosities relations of SPIRE observations of the galaxies were studied extensively. The limited parameters (for example; galaxy name, Far-infrared luminosity L_{FIR} and distance luminosity D_l) were extracted from new observations of a recent paper [2], while the redshifts of galaxies measured by Doppler-shifted (z), Far-infrared fluxes at 60 μm and 100 μm (F_{60} and F_{100} μm) were taken from NASA/IPAC Extragalactic Database (NED) [10]. The calculated parameters (name galaxy, $\log L_{FIR}$, D_l , z , F_{60} , and F_{100}) of each selected galaxy are listed in Table-1.

Table 1- Data obtained from [2] and NASA/IPAC Extragalactic (NED) of the parameters used in our analysis.

| No | Name Galaxy | $\text{Log}L_{\text{FIR}} (L_{\odot})$ | D_l (Mpc) | z | F60 (Jy) | F100 (Jy) | Morphological Type |
|----|------------------|--|-------------|----------------------|----------|-----------|--------------------|
| 1 | NGC 0023 | 10.9 | 68 | 0.01524 | 9.03 | 15.66 | Sa |
| 2 | NGC 34 | 11.2 | 85 | 0.02000 | 17.05 | 16.86 | S0-a |
| 3 | IRAS 00188-0856 | 12.2 | 591 | 0.12800 | 2.592 | 3.403 | Galaxy or QSO* |
| 4 | ESO 350-IG038 | 10.8 | 87 | 0.02100 | 6.88 | 5.04 | Irr** |
| 5 | IRAS 00397-1312 | 12.6 | 1285 | 0.26100 | 1.832 | 1.904 | Galaxy or QSO |
| 6 | NGC 0232 | 11.2 | 95 | 0.02300 | 10.05 | 15.75 | SBa |
| 7 | NGC 253 | 10.3 | 3 | 0.00100 | 967.81 | 1288.15 | SABc |
| 8 | I Zw 1 | 11.4 | 272 | 0.06000 | 2.161 | 1.749 | Sc |
| 9 | NGC 0317B | 11 | 80 | 0.01771 | 9.34 | 13.95 | SBbc |
| 10 | IRAS 01003-2238 | 11.9 | 539 | 0.11800 | 2.287 | 1.79 | Galaxy or QSO |
| 11 | IC 1623 | 11.4 | 86 | 0.01900 | 23.85 | 31.53 | S? |
| 12 | ESO 244-G012 | 11.1 | 95 | 0.02290 ₃ | 9.27 | 11.76 | Sc |
| 13 | CGCG 436-030 | 11.5 | 138 | 0.03100 | 10.71 | 9.67 | Sbc |
| 14 | Mrk 1014 | 12.3 | 763 | 0.16300 | 2.348 | 1.915 | Galaxy or QSO |
| 15 | NGC 0828 | 11.1 | 80 | 0.01792 ₆ | 11.46 | 25.33 | Sa |
| 16 | NGC 0891 | 10.2 | 10 | 0.00176 | 66.46 | 172.23 | Sb |
| 17 | UGC 01845 | 10.9 | 70 | 0.01514 | 10.31 | 15.51 | Sab |
| 18 | NGC 0958 | 10.9 | 82 | 0.01915 | 5.85 | 15.08 | SBc |
| 19 | NGC 1056 | 9.7 | 24 | 0.00515 ₄ | 5.33 | 10.2 | Sa |
| 20 | NGC 1097 | 10.4 | 16 | 0.00424 | 58.29 | 116 | SBb |
| 21 | IRAS 03158+4227 | 12.4 | 623 | 0.13400 | 4.256 | 4.276 | Galaxy or QSO |
| 22 | 3C 84 | 10.8 | 78 | 0.01756 | 7.09 | 7.6 | S0 |
| 23 | NGC 1482 | 10.5 | 25 | 0.00620 ₆ | 33.36 | 46.73 | S0-a |
| 24 | IRAS 03521+0028 | 12.3 | 709 | 0.15191 | 2.638 | 3.833 | Galaxy or QSO |
| 25 | UGC 02982 | 10.9 | 77 | 0.01771 | 8.38 | 16.82 | SABa |
| 26 | ESO 420-G013 | 10.7 | 49 | 0.01191 | 13.66 | 20.88 | S0-a |
| 27 | NGC 1572 | 11 | 86 | 0.02039 ₄ | 8.03 | 16.81 | SBa |
| 28 | NGC 1614 | 11.3 | 68 | 0.01600 | 32.12 | 34.32 | SBc |
| 29 | UGC 03094 | 11.1 | 108 | 0.02470 | 6.35 | 12.85 | Sab |
| 30 | MCG-05-12-006 | 10.9 | 78 | 0.01875 | 8.15 | 9.404 | SBb |
| 31 | IRAS F05189-2524 | 11.8 | 185 | 0.04256 | 13.25 | 11.84 | E** |
| 32 | IRAS09022-3615 | 12 | 411 | 0.05960 | 11.64 | 11.08 | Galaxy or QSO |
| 33 | NGC 2764 | 10 | 40 | 0.00907 | 3.67 | 7.224 | S0 |

| | | | | | | | |
|----|---------------------|------|-----|--------------|--------|--------|------------------|
| 34 | M81 | 9.2 | 4 | 0.00090 | 6.806 | 32.03 | Sab |
| 35 | NGC 3077 | 7.7 | 1 | 0.00005 | 15.9 | 26.53 | S? |
| 36 | NGC 3221 | 10.7 | 61 | 0.01370 | 7.72 | 18.76 | Sc |
| 37 | IRAS F10565+2448 | 11.8 | 192 | 0.04300 | 12.1 | 15.01 | Irr |
| 38 | NGC 3627 | 10.2 | 12 | 0.00243 | 66.31 | 136.56 | Sb |
| 39 | ESO 320-G030 | 11 | 45 | 0.01084 | 34.38 | 46.28 | SABa |
| 40 | NGC 4051 | 9.5 | 14 | 0.00234 | 10.53 | 24.93 | SABb |
| 41 | NGC 4459 | 9.1 | 19 | 0.00396 | 1.87 | 4.82 | S0 |
| 42 | NGC 4569 | 7.5 | 1 | 0.00510 | 9.8 | 26.56 | Sab |
| 43 | NGC 4710 | 9.6 | 18 | 0.00375 | 5.89 | 13.21 | S0-a |
| 44 | NGC 4736 | 9.9 | 8 | 0.00105 | 71.54 | 120.69 | SABa |
| 45 | NGC 5010 | 10.6 | 43 | 0.02100 | 10.29 | 21.69 | S0-a |
| 46 | NGC 5104 | 10.9 | 82 | 0.01855 | 6.78 | 13.37 | Sa |
| 47 | IRAS 14378-3651 | 11.9 | 303 | 0.06760 | 6.72 | 8.08 | Galaxy or QSO |
| 48 | NGC 5866 | 9.4 | 14 | 0.00225 | 5.26 | 16.98 | S0-a |
| 49 | IRAS 16090-0139 | 12.3 | 618 | 0.13400 | 3.609 | 4.874 | Galaxy or QSO |
| 50 | PG 1613+658 | 11.5 | 600 | 0.12900 | 0.635 | 1.002 | E |
| 51 | IRAS F16399-0937 | 11.3 | 118 | 0.02701 2 | 8.42 | 14.72 | Galaxy or QSO |
| 52 | NGC 6240 | 11.6 | 108 | 0.02450 | 22.94 | 26.49 | S0-a |
| 53 | NGC 6701 | 10.9 | 62 | 0.01320 | 10.05 | 20.05 | Sa |
| 54 | IRAS 19254-7245 | 11.8 | 270 | 0.06170 9 | 5.16 | 5.789 | Galaxy or QSO |
| 55 | IRAS 20100-4156 | 12.4 | 595 | 0.13000 | 5.19 | 5.165 | Galaxy or QSO |
| 56 | MCG+04-48-002 | 10.9 | 65 | 0.01400 | 8.15 | 12.5 | Sd |
| 57 | NGC 6946 | 9.8 | 5 | 0.00015 | 129.78 | 290.69 | SABc |
| 58 | IRAS 20414-1651 | 12 | 392 | 0.08600 | 4.364 | 5.247 | Galaxy or QSO |
| 59 | IC 5063 | 10.2 | 46 | 0.01130 | 5.87 | 4.25 | S0-a |
| 60 | CGCG 448-020 | 11.7 | 161 | 0.03610 | 12.65 | 11.76 | S0-a |
| 61 | NGC 7582 | 10.5 | 21 | 0.00500 | 52.25 | 82.86 | SBab |
| 62 | IRAS 23230-6926 | 12.1 | 482 | 0.10700 | 3.744 | 3.42 | Galaxy or QSO |
| 63 | IRAS 23365+3604 | 12 | 290 | 0.06450 | 7.44 | 9.01 | Galaxy or QSO |
| 64 | NGC 7771 | 11.1 | 63 | 0.01400 | 20.93 | 44.85 | Sa |
| 65 | Mrk331 | 11.2 | 81 | 0.01848 | 18.43 | 22.56 | Sa |

Note: * QSO=Quasar and ** Irr=Irregular galaxy; E= Ellipticals.

Statistical procedures

The statistical software ,statistic-win-program, was utilized to process and analyze various relationships between variables and calculate whether toughness of regression exists between the behaviors of the two variables. This association is also represented in the form of scattering graphs. The linear partial correlation (R) coefficient values range from + 1 to -1 [11, 12]. A regression value

of ±1 refers that the two functions are perfectly correlated. Indeed, when the value of the measurement of R is or close to zero, there is a weak regression correlation between the two components.

Description Parameters

In general, the term luminosity of the CO line was calculated from the integrated intensity S_{co} in Jy $Km s^{-1}$, and beam solid angle $\Omega_b = \pi\theta_B^2/4ln2$ (θ_B in radians). The CO line luminosity can be found by [13, 14]:

$$L_{co} = \frac{\Omega_b S_{co} D_l^2}{(1+z)^3} \quad (\text{in } K \text{ km } s^{-1} pc^2) \dots \dots \dots (1)$$

where D_l is the distance of cosmological luminosity in megaparsec (Mpc) described by standard cosmological parameters including Hubble constant H_0 , matter density parameter Ω_M , and a parameter of cosmological constant density Ω_Λ , and can be determined by [13]:

$$D_l = (1+z) \frac{c}{H_0} \int_0^z \frac{dz}{[\Omega_M(1+z)^3 + \Omega_\Lambda]^{1/2}} \dots \dots \dots (2)$$

By substituting equation (2) in equation (1), the CO line luminosity (L_{co}) takes the form:

$$L_{co} = \left(\frac{c}{H_0}\right)^2 \frac{\Omega_b S_{co}}{(1+z)} \cdot \frac{z}{[\Omega_M(1+z)^3 + \Omega_\Lambda]^{1/2}} \dots \dots \dots (3)$$

where c is the speed of light.

For galaxies without strong interactions, the following relationship between L_{FIR} and L_{CO} is constructed by [15, 16]:

$$\frac{L_{FIR}}{10^9} L_\odot = 31 \left[\frac{L_{CO}}{10^9} L_\odot \right]^{0.74} \dots \dots \dots (4)$$

and could be written in the form:

$$\left[\frac{(L_{FIR} / 10^9) L_\odot}{31} \right]^{1.35} = \frac{L_{CO}}{10^9} L_\odot \dots \dots \dots (5)$$

The logarithmic scale of equation (5) is written as:

$$\text{Log } L_{CO} = 1.35 \text{Log } L_{FIR} - 5.2 \dots \dots \dots (6)$$

Here L_{CO} and L_{FIR} are given in the solar luminosity unit (L_\odot).

The molecular hydrogen gas mass M_{H_2} in solar mass (M_\odot) is derived with the use of the formula [14-17]:

$$M_{H_2}(M_\odot) = \alpha_{CO} L_{CO}(L_\odot) \dots \dots \dots (7)$$

where α_{CO} is the CO line luminosity-to- molecular gas mass conversion factor. The conversion factor α_{CO} is almost constant and equal to $\alpha_{CO} \approx 0.6 - 5$ in unit $M_\odot (K \text{ km } s^{-1} pc^2)^{-1}$ [14-19]. The value of α_{CO} that is used in this study is $\sim 4.8 M_\odot (K \text{ km } s^{-1} pc^2)^{-1}$ [15-17].

From equations 6 and 7, we have:

$$\text{Log } M_{H_2}(\text{in unit } M_\odot) = 1.35 \text{log } L_{FIR}(L_\odot) - 4.5 \dots \dots \dots (8)$$

4- The logarithmic scale of MHI in M_\odot can be calculated as follows [15]:

$$\text{Log } MHI(\text{in unit } M_\odot) = 0.61 \text{log } L_{FIR}(L_\odot) + 3.08 \dots \dots \dots (9)$$

The dust temperature T_d in (K^0) is given roughly by [20, 21]:

$$T_d \approx 49 \left(\frac{F_{60\mu m}}{F_{100\mu m}} \right)^{0.4} \dots \dots \dots (10)$$

where $F_{60 \mu m}$ and $F_{100 \mu m}$ are IRAS Far- infrared band fluxes at 60 μm and 100 μm in unit Jansky (Jy), where $1 \text{ Jy} = 10^{-26} \text{ W} \cdot \text{m}^{-2} \cdot \text{Hz}^{-1}$ (in units SI).

The dust mass of galaxies M_{dust} in the solar mass unit can be estimated by integrating the temperature database with the Far-infrared flux rates of $F_{60 \mu m}$ and $F_{100 \mu m}$ [20, 22]:

$$M_{dust} (M_\odot) = 0.00478 \cdot F_{100}(mJy) \cdot D_l^2 \cdot \left\{ e \left[2.94 \left(\frac{F_{100\mu m}}{F_{60\mu m}} \right)^{0.4} \right] - 1 \right\} \dots \dots \dots (11)$$

We can re-write equation (10) as:

$$\left(\frac{F_{100\mu m}}{F_{60\mu m}} \right)^{0.4} = \frac{49}{T_d}$$

The substitution of the term $\frac{49}{T_d}$ instead of $(\frac{F_{100\mu m}}{F_{60\mu m}})^{0.4}$ in equation (11) yields:

$$M_{dust} (M_{\odot}) = 4.78 F_{100} (Jy) D_l^2 \{e^{144/T_d} - 1\} \dots \dots \dots (12)$$

7- The star formation rate (SFR) is calculated in Far-infrared bands (60-100 μm) from the relation [23]:

$$SFR_{FIR} = \left(\frac{L_{FIR}}{5.7 * 10^9 L_{\odot}} \right) \quad (in M_{\odot} yr^{-1}) \dots \dots \dots (13)$$

8- Lifetime gas depletion (t_{gas}) which is usually measured in years and caused by high mass star formation (without mass recycling by supernovae or other mass losses) is calculated as follows [16]:

$$t_{gas} = 5 * 10^{10} \left(\frac{L_{CO}}{L_{FIR}} \right) \quad (in unit yr) \dots \dots \dots (14)$$

Results and Discussion

This work studied the relationships between Far-infrared, CO emission line luminosities, star formation rates in the Far-infrared band and masses of atomic hydrogen (MHI)+molecular hydrogen (MH₂) of a *Herschel SPIRE FTS* galaxies sample. The results of the comparison between the cold gas content and luminosities revealed different effects.

The results of statistical analysis showed that the mean value \pm standard error of LogL_{FIR} is equal to 10.93 ± 0.12 ($L_{FIR}=8.5 \times 10^{10} L_{\odot}$) for our sample galaxies. These galaxies have a higher Far-infrared luminosity with a lower limit of about $\approx 3.2 \times 10^{10} L_{\odot}$ and an upper quartile which is equal to $5 \times 10^{11} L_{\odot}$. The calculations showed a very strong relationship $L_{FIR} \propto (MHI+MH_2)^{1.11 \pm 0.024}$ with a very strong positive partial correlation coefficient ($R=0.98$) and a very high probability level ($p \leq 10^{-7}$), where p is the probability of chance correlation. Figure-1a shows that the slope is linear and steeper than unity. This study also revealed that the total mass of cold gas (MHI+MH₂) and CO/ FIR luminosities, along with their relative H₂ and HI content alone, are the factors that indicate the actual meaning of the gas.

The relationships among the logarithm dust mass, L_{CO}/L_{FIR} ratio, and MHI+MH₂ of these galaxies were studied. The statistical analysis results showed significant relationships between (Log L_{CO}/L_{FIR} , Log M_{dust}) and Log (MHI+MH₂) with a very strong partial correlation coefficient ($R \approx 1$) and a very high probability ($p \leq 10^{-7}$), where Figure-1b reveals that the slope is almost linear (Slope > 1). The L_{CO} to L_{FIR} ratio provides a qualitative measure of star formation activity in the interaction of galaxies, where the average value $\langle L_{CO}/L_{FIR} \rangle = 0.05$. These galaxies have higher infrared luminous than CO emission. We can conclude that CO emissions will be very essential for studying the central region's gas kinematics and dynamics. Thus, the star formation rate is related to the total gas mass of galaxies.

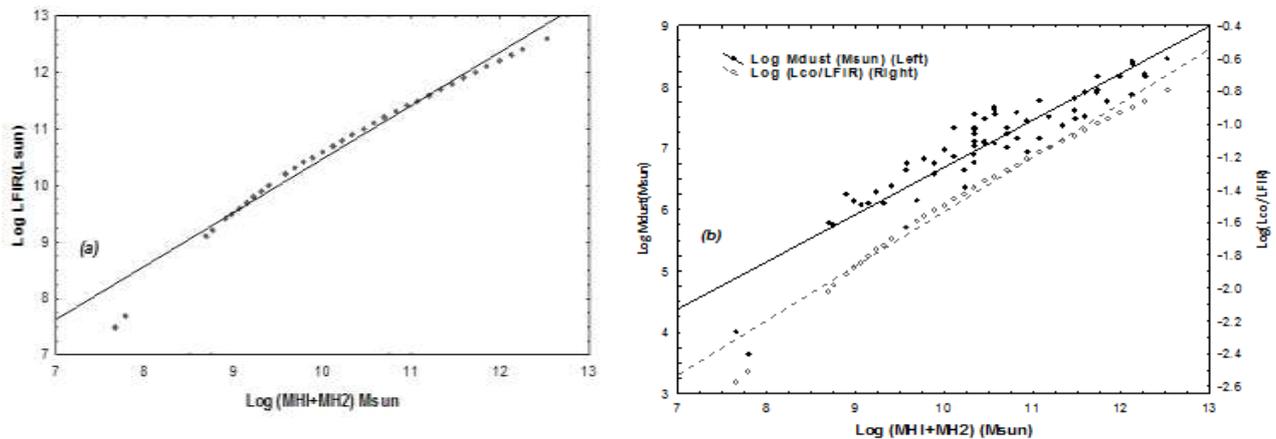


Figure 1- (a) Far-Infrared luminosity Log L_{FIR} as a function of total cold gas (MHI+MH₂), in solar units. The solid line represents the linear correlation regression. (b) The relationship between dust mass of galaxies M_{dust} (on the left), ratio L_{CO}/L_{FIR} (on the right) and MHI+MH₂. The straight black line represents the fitting to all the data for M_{dust} and the dashed line represents the fitting to the all data for L_{CO}/L_{FIR} versus MHI+MH₂, respectively.

Figure-2a (left panel) demonstrates that the ratio $\text{Log} (L_{\text{FIR}}/\text{MH}_2)$ and dust temperature T_d indicate a clear negative relationship with a correlation coefficient of ($R \approx -0.46$) and a good probability value ($p \approx 10^{-4}$). It should be pointed out here that the slope of the line is $\approx 0.4 \pm 0.09$. The value of the ratio of Far-infrared emission luminosity to molecular gas implies that the SFR strongly depends on the dust temperature (T_d). The significant relationship between $L_{\text{FIR}}/\text{MH}_2$ ratio and T_d supports essentially that the Far-infrared emission comes from the merged dust with the molecular clouds.

The mean values of the logarithmic scale of cold gas masses (MHI, MH_2) of our sample were 9.75 ± 0.08 , 10.26 ± 0.17 , and 7.06 ± 0.11 , whereas those for the M_{dust} were $5.6 \times 10^9 M_\odot$, $1.8 \times 10^{10} M_\odot$, and $1.1 \times 10^9 M_\odot$, respectively. Figure-2b (right panel) shows a linear relationship, implying that the correlation between molecules gas to dust masses and dust temperature ($\text{Log} (\text{MH}_2/M_{\text{dust}})$, T_d) is positive and very strong ($R \approx 0.87$) with a stronger probability ($p \leq 10^{-7}$). The used linear regression equation is given by:

$$\text{LogMH}_2/M_{\text{dust}} = S T_d + m,$$

where S is the slope and m is the intercept with the y-axis. It should be noted that the best representation is obtained by a minimum standard error which is clarified in the form of: $\text{LogMH}_2/M_{\text{dust}} = (0.75 \pm 0.05)T_d + (1.74 \pm 0.27)$. Figure-2b (solid black line), which describes the relationship between ($\text{Log MHI}/M_{\text{dust}}$) and (T_d), shows that $R \approx 0.45$, $p \approx 10^{-4}$, and the slope of the solid line is ≤ 0.5 . The comparison between the ratio $\text{MHI}/M_{\text{dust}}$ and the T_d indicates that the resulted ratio varies from a galaxy to another and that the dust is regarded as an indicator of gas in its atomic and molecular forms.

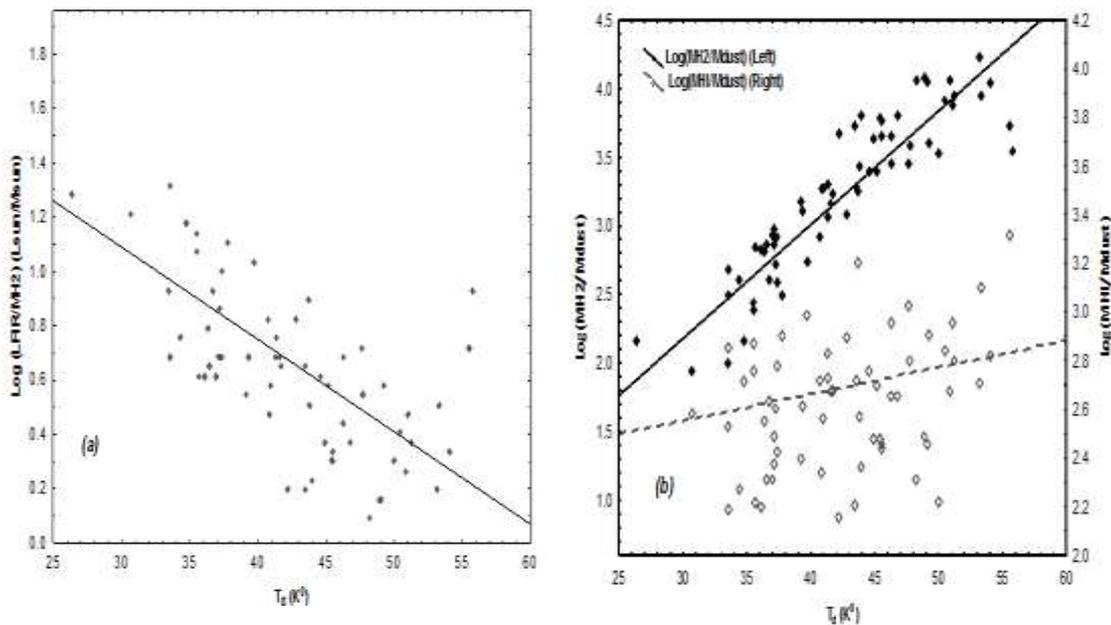


Figure 2- (a) The relationship between ratio $L_{\text{FIR}}/\text{MH}_2$ (L_\odot / M_\odot) and dust temperature T_d (K^0). (b) The relationship between ratios $\text{MH}_2/M_{\text{dust}}$ (on the left) and $\text{MHI}/M_{\text{dust}}$ (on the right) as a function of T_d . The straight black line represents the fitting to all the data for $\text{MH}_2/M_{\text{dust}}$ and the dashed line represents fitting to all the data for $\text{MHI}/M_{\text{dust}}$ versus T_d .

This work studied the relationship between the ratio masses of molecular hydrogen to dust content ($\text{MH}_2/M_{\text{dust}}$) and the Far-infrared luminosity of galaxies. The results of the statistical analysis showed a strong relationship between $\text{Log} (\text{MH}_2/M_{\text{dust}})$ and $\text{Log} L_{\text{FIR}}$ with a positive and very strong correlation coefficient ($R \approx 0.84$) and a higher probability ($p \leq 10^{-7}$). The ratio $\text{MH}_2/M_{\text{dust}}$ is used as a function of the Far-infrared luminosity in Figure-3a (left panel), which demonstrates that the relationship is taking the form: ($\text{MH}_2/M_{\text{dust}} \propto L_{\text{FIR}}^{0.84 \pm 0.08}$). The ratio $\text{MH}_2/M_{\text{dust}}$ is also taken as a function of the dust temperature in (Figure-2b left). Both figures showed that the ratio does not depend on the type of

morphology of the galaxies, which was also confirmed by previous results [i.e. 7, 15 and 16]. Our results indicate that dust may be associated with the stars emerging in the central bulges of such galaxies, which leads to increasing the dust mass and reducing the cold gas to dust mass ratio.

The relationship between L_{CO}/L_{FIR} and T_d , as shown in Figure-3b (right panel), showed a correlation coefficient of $R \approx 0.5$, probability of $p \approx 10^{-4}$, and slope of $\sim 0.23 \pm 0.06$. The results indicate a weak relationship, due to the effect of distance D_1 or redshift z based on *Malmquist bias* (the effect of distance dependence selection) between the parameters in this sample (see equations 1 and 3).

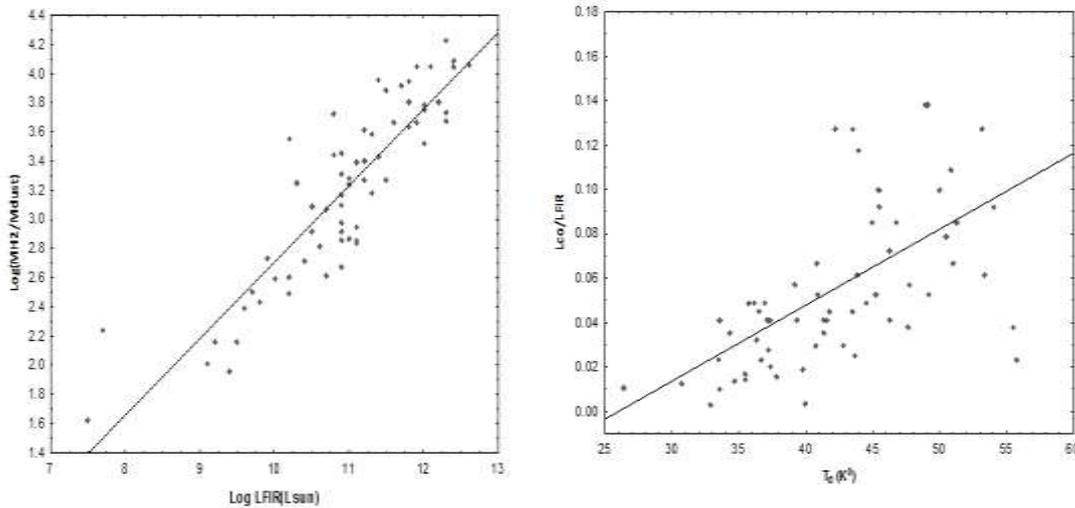


Figure 3-(a) The ratio M_{H_2}/M_{dust} as a function of L_{FIR} . (b) The ratio CO line emission (L_{CO}) to Far-infrared emission (L_{FIR}) luminosities as a function of T_d .

Now we discuss the relationship between the atomic and molecular gas to dust masses and gas depletion lifetime (t_{gas}). It was found that the linear regression of Figure-4a (left panel) is taking the form: $Log MH_2/M_{dust} = (1.3 \pm 0.15) t_{gas} + (2.26 \pm 0.09)$ while for Figure-4b (right panel) it is: $Log MH_I/M_{dust} = (-0.72 \pm 0.25) t_{gas} + (2.99 \pm 0.08)$. There is an interesting relationship between these quantities with a strong positive correlation coefficient ($R \approx 0.73$) and a very high probability ($p \leq 10^{-7}$) between $Log (MH_2/M_{dust})$ and t_{gas} . A negative relationship between $Log (MH_I/M_{dust})$ and t_{gas} was also observed, with a partial correlation value of $R \approx -0.33$ and a significance probability ($p = 6 \times 10^{-3}$). Based on a sample of extragalactic spectra, we show that the cold gas depletion lifetime is dependent on high star formation efficiency (SFE) with extreme L_{co}/L_{FIR} ratio in these galaxies, indicating that the star formation process can only be enhanced by very strong interactions between galaxies.

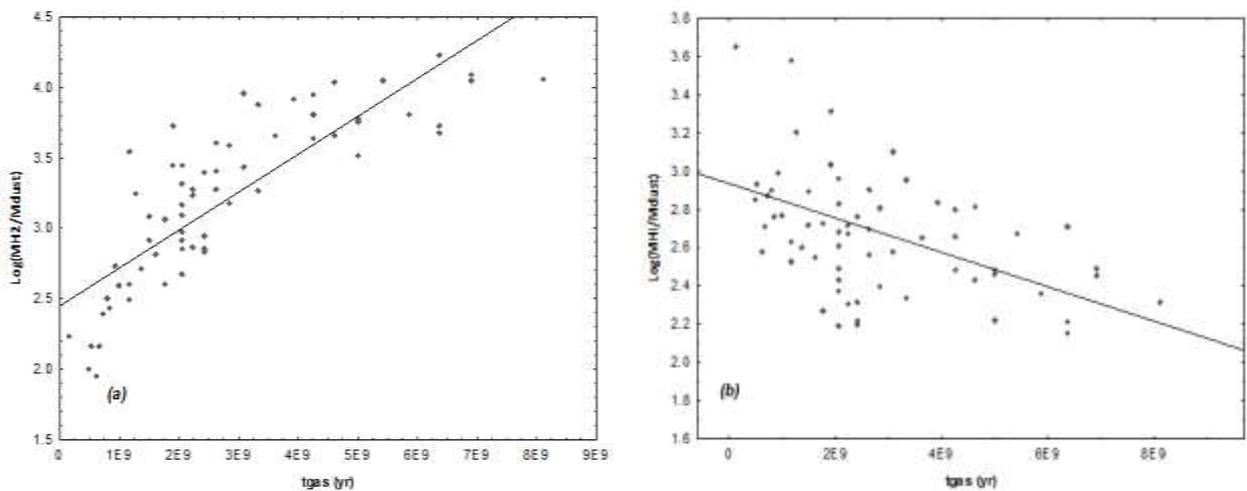


Figure 4- (a) The ratio M_{H_2}/M_{dust} versus lifetime gas depletion t_{gas} in years unit. (b) The ratio M_{HI}/M_{dust} versus t_{gas} .

In this work, we also studied the relationships between the mass dust of galaxy (M_{dust}) and ratio mass MHI/MH₂, CO-luminosity (L_{co}), star formation rate in Far-infrared band (SFR_{FIR}). The results showed mean values of $\text{Log MHI/MH}_2 = -0.51 \pm 0.09$, $\text{Log } L_{\text{co}} = 9.57 \pm 0.17$ ($L_{\text{co}} \approx 3.7 \times 10^9 L_{\odot}$), and $\text{SFR}_{\text{FIR}} = 44.25 M_{\odot} \text{ yr}^{-1}$ for our sample galaxies. The existence of a negative correlation between MHI/MH₂ ratio and M_{dust} was recorded, with a partial coefficient of $R \approx -0.9$. For a slope ≈ -1 , we have the $\text{Log } M_{\text{dust}}$ is inversely proportional to $\text{Log (MHI/MH}_2)$. It can also be noticed that if the HI / H₂ ratio mass is less than or equal to 1 ($\text{MHI} / \text{MH}_2 \leq 1$), there is a systematic variation in the HI content, while the deficiency of MHI as the relative abundance of the molecular component (MH₂) increases.

The results also showed a very strong linear correlation between $\text{Log } L_{\text{co}}$ and $\text{Log } M_{\text{dust}}$ with a correlation coefficient of $R=0.92$, a very strong probability ($p \leq 10^{-7}$), and a Slope $\sim 0.86 \pm 0.04$. In terms of statistics, we deduce a tight linear relationship between M_{dust} and SFR_{FIR} (Slope ~ 1). For these galaxies, star formation rate in the Far-infrared radiation band (SFR_{FIR}) is strongly related to their dust content, which is relevant for galaxies involving a wide range of the FIR luminosity. We also found a statistically significant relationship with a clear positive correlation between these parameters ($R \approx 0.5$), with a good probability level ($p = 2 \times 10^{-5}$). In Figures-(5a, 5b) and 6, we examine the $\text{Log } M_{\text{dust}}$ versus Log MHI/MH_2 , $\text{Log } L_{\text{co}}$ versus $\text{Log } M_{\text{dust}}$, and M_{dust} versus SFR_{FIR} , respectively. The MH₂ derived from the CO surface brightness is more strongly linked with the M_{dust} than the MHI surface mass, however, the dust mass association of the molecular content is not significant. Therefore, cold dust emission is probably correlated with both of the atomic and molecular forms in these galaxies. In fact, the dust mass is often related to the MHI+MH₂. Our findings from this analysis are consistent with those of previous articles [7, 9, 15, 16].

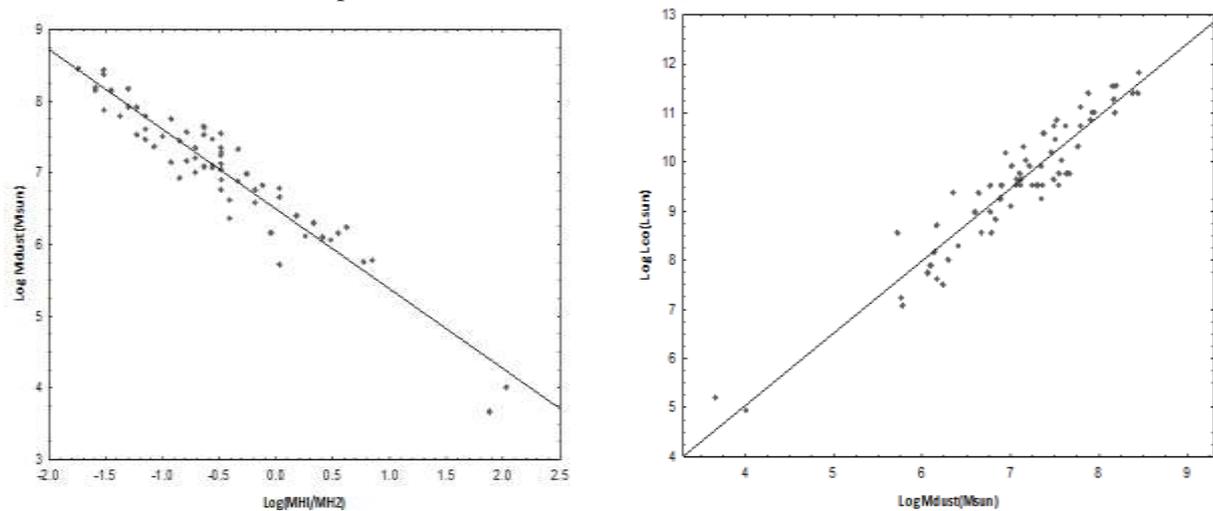


Figure 5- (a) The M_{dust} (M_{\odot}) as a function of the ratio MHI/MH₂. (b) The CO line luminosity versus M_{dust} , on a scale of logarithms.

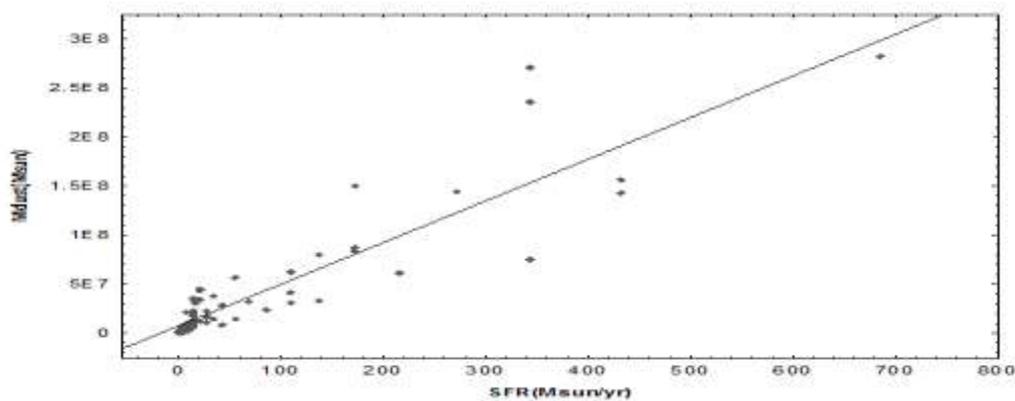


Figure 6- The mass dust M_{dust} versus star formation rate in ($M_{\odot} \text{ yr}^{-1}$).

The results of regression analysis show that the logarithmic ratio of $L_{\text{FIR}}/\text{MH}_2$ to F_{100}/F_{60} is apparently positive and well correlated ($R \sim 0.5$) and that their relationship is not linear ($L_{\text{FIR}}/\text{MH}_2 \propto F_{100}/F_{60}^{0.4 \pm 0.09}$), as demonstrated in Figure-7a (left panel). This indicates that the Far- infrared luminosity for each unit of the molecular gas mass is an indicator of the star formation rate as it is directly related to infrared luminosity, where star formation activity occurs within the molecular clouds as an indication of the cold dust temperature component (which is mainly mixed with the HI gas). The parameter $\log(F_{100}/F_{60})$ is introduced because the real situation is more complicated and because it provides a reliable indication of the dust temperature between 26.37 K^0 and 55.76 K^0 which is based on the power-law emission adopted (i.e. $B_\lambda \propto \lambda^n$, with $n=0$).

Figure-7b (right panel) reveals the variation of the cold dust temperature with the parameter (F_{100}/F_{60}). These results are consistent with previously reported findings [1].

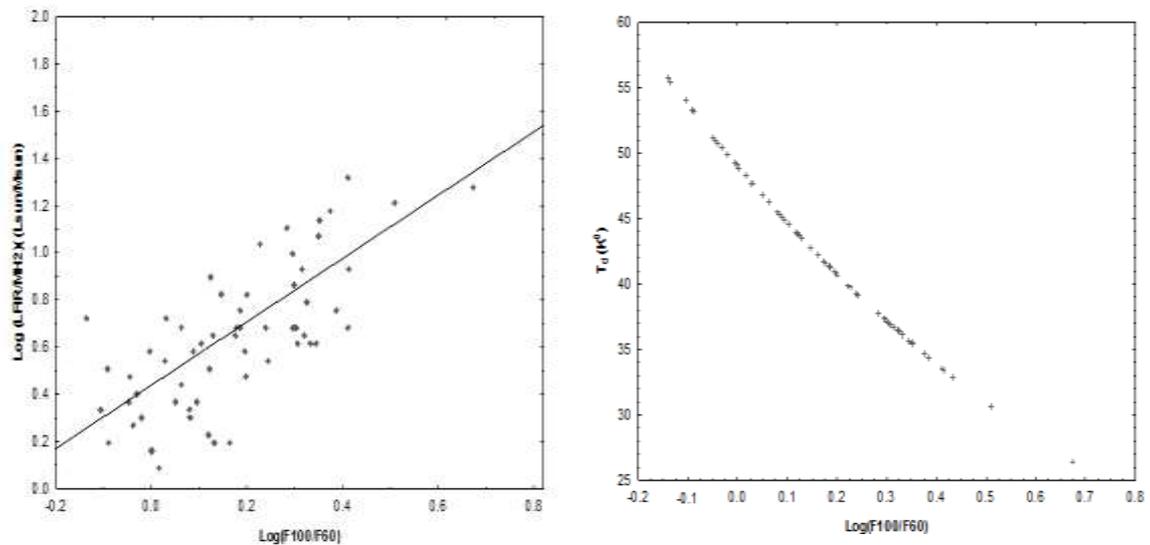


Figure 7- (a) The relationship between ratio $L_{\text{FIR}}/\text{MH}_2$ in (L_\odot/M_\odot) and the flux ratio F_{100}/F_{60} . **(b)** The cold dust temperature T_d (K^0) as a function of ratio F_{100}/F_{60} for $n=0$.

Conclusion

On the basis of our statistical analysis, we infer that the molecular and atomic hydrogen contents are related to a linear relationship (Slope ~ 1) with the hotter dust mass, but the correlation in the case of molecular gas is stronger. This refers to the abundance of dust in the case of atomic and molecular gas produced in the Far-infrared wavelengths band ($60 - 100 \mu\text{m}$). We found, based on the statistical analysis, that the average value of the ratio $\text{MH}_2/M_{\text{dust}}$ is $1.8 \times 10^{10} M_\odot$. The results also indicated that far-infrared emission has a tight relationship with all variables, which illustrates the presence of recent starburst which is in turn an indicative of the star formation activity, as Far-infrared luminosity (L_{FIR}) is related with the mass of molecular hydrogen and star formation rate (SFR_{FIR}) in this type of galaxies directly.

We observed the difference of the correlation in FIR- infrared luminosity and CO luminosity with other parameters in our sample, that is, the mean value of L_{FIR} ($L_{\text{FIR}} \sim 10^{11} L_\odot$) is larger than that in L_{CO} ($L_{\text{CO}} \approx 10^9 L_\odot$). This work also revealed that the actual meaning of the gas is indicated by the total mass of cold gas and CO to FIR emission spectra that are related with the molecular hydrogen material MH_2 , while increasing Far-infrared luminosity leads all these parameters to increase. The ratio F_{100}/F_{60} is an indicator of the cold dust temperature T_d . The value of dust temperature was in the range of $26.37 - 55.76 \text{ K}^0$. Depending on the power-law emission ($B_\lambda \propto \lambda^n$), it was found that the increase in cold dust temperature is associated with increasing the star formation activity.

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